

# Expectations and Credit Slumps

Antonio Falato

Federal Reserve Board

Jasmine Xiao

University of Notre Dame

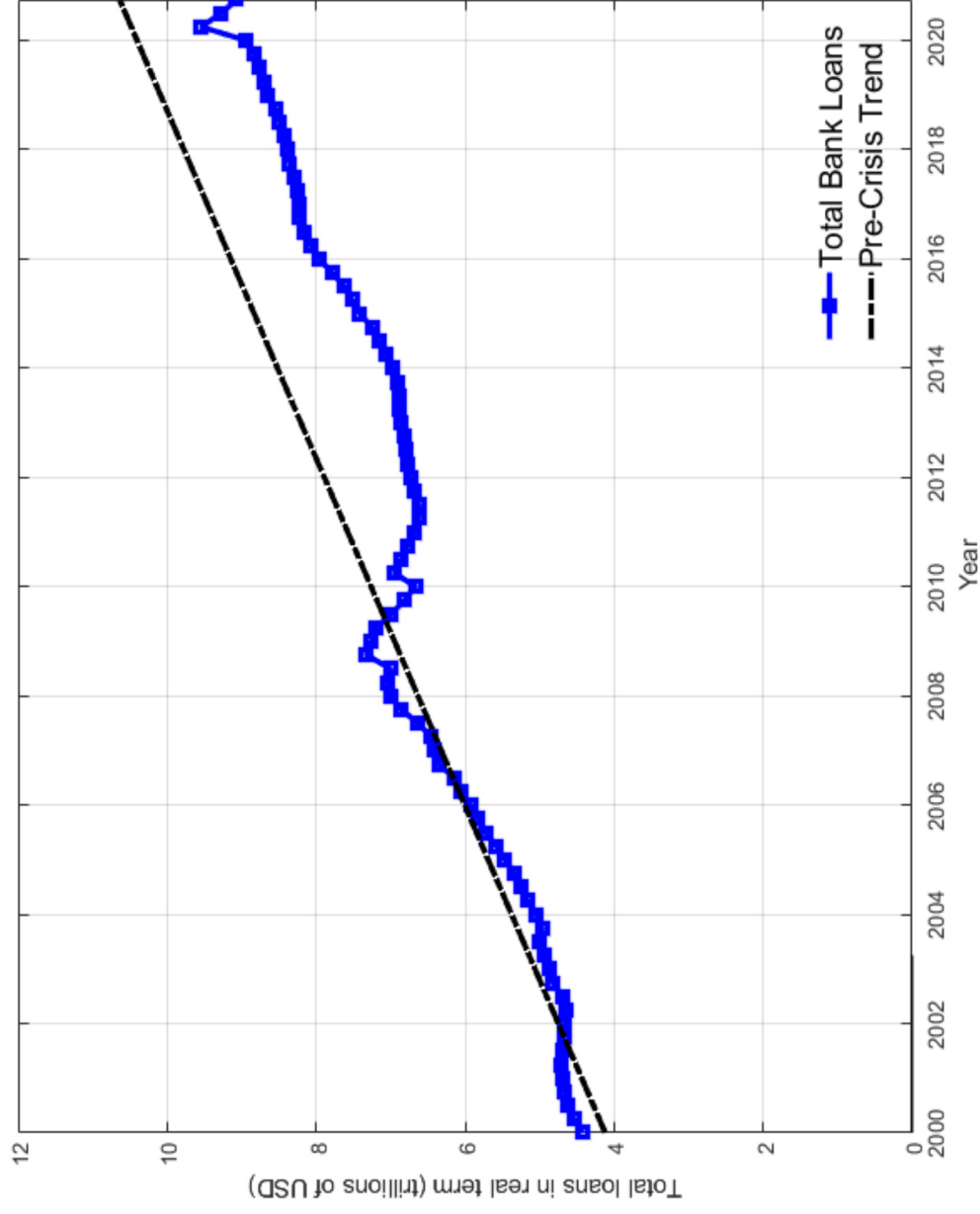
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*Disclaimer: The views expressed in this paper are those of the authors and do not necessarily reflect the views of the Federal Reserve Board of Governors or the Federal Reserve System.*

## Question

- Why was bank lending so slow to recover after the 2008-09 financial crisis?



Sources: H.8 Assets and Liabilities of Commercial Banks in the U.S.

## Our Explanation

- Banks over-extrapolate the past: they remained over-pessimistic long after 2009
- And persistent pessimism was a drag on their lending

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## This Paper

- Uses new survey data to measure individual banks' expectations

Expectations & Real Outcomes: Greenwood and Schleifer (2014), Coibion and Gorodnichenko (2015), Angeletos et al. (2020), Bordalo et al. (2020), Rozsypal and Schlafmann (2020), Kohlhas and Walther (2021), Giglio et al. (2021), Ma et al. (2021), Farmer et al. (2022)

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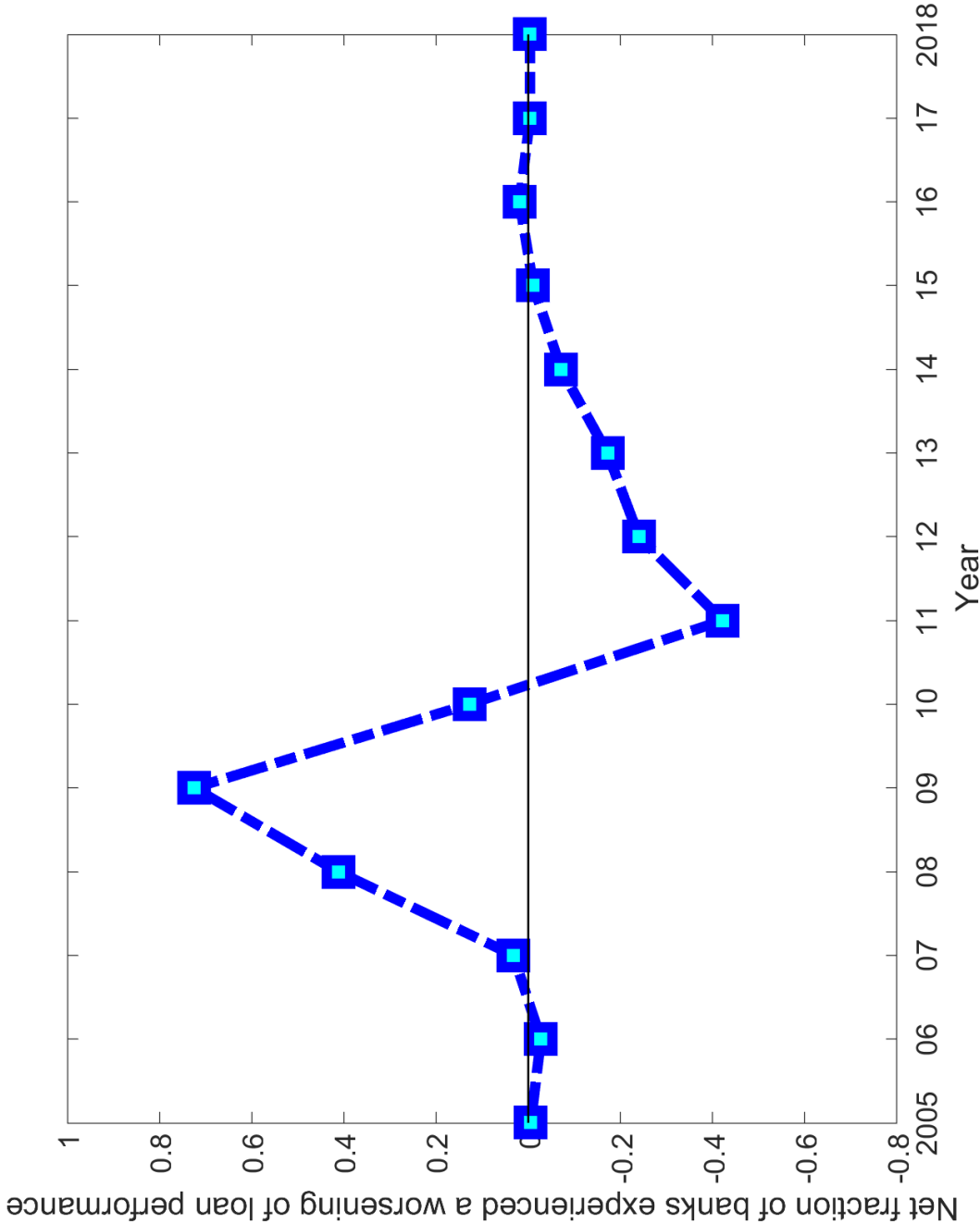
## This Paper

- Uses new survey data to measure individual banks' expectations
- Constructs a model to quantify the macroeconomic consequences of distorted bank expectations

Expectations & Real Outcomes: Greenwood and Schleifer (2014), Coibion and Gorodnichenko (2015), Angeletos et al. (2020), Bordalo et al. (2020), Rozsypal and Schlafmann (2020), Kohlhas and Walther (2021), Giglio et al. (2021), Ma et al. (2021), Farmer et al. (2022)

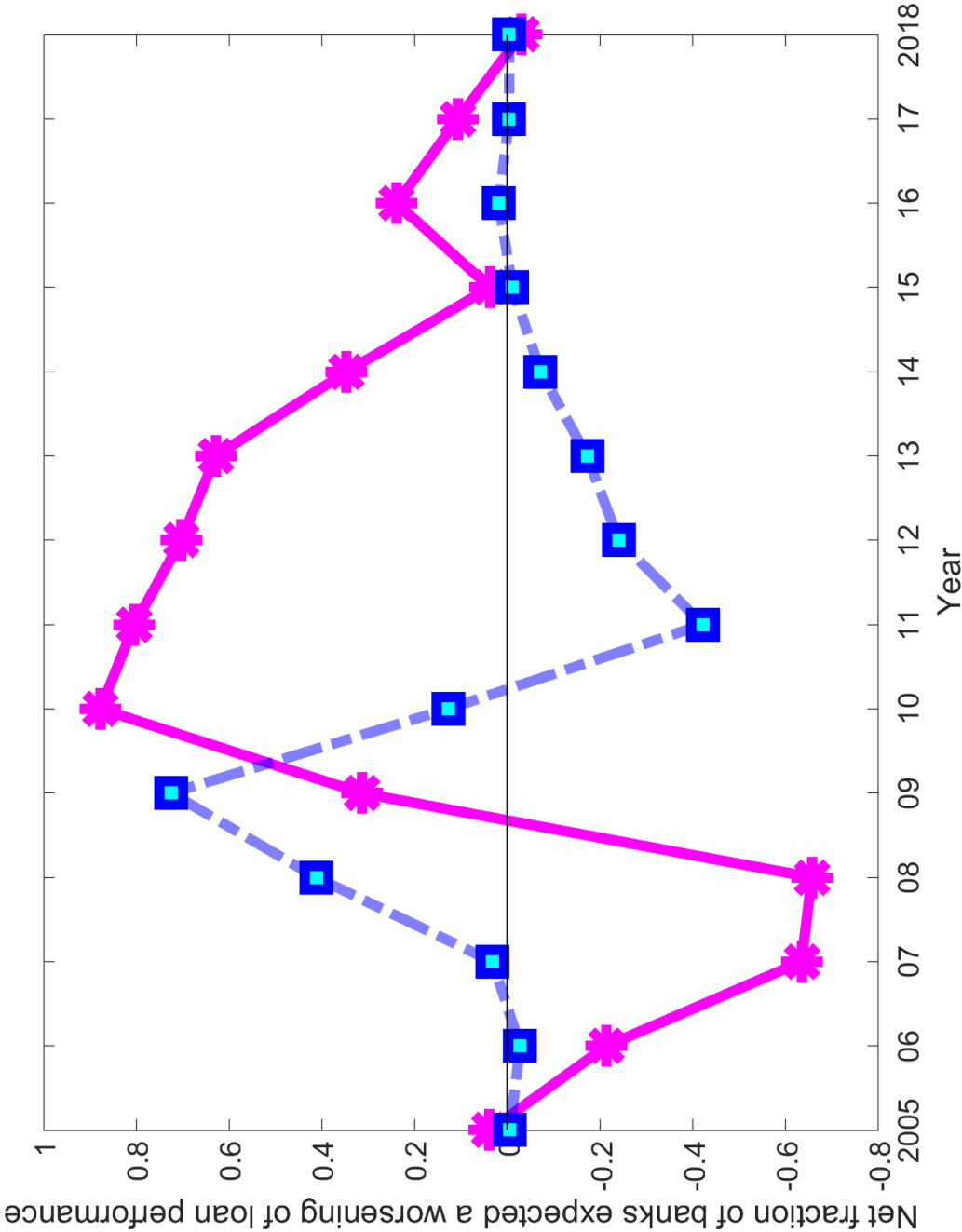
Expectations in Credit & Business Cycles: Krishnamurthy and Li (2020), Bordalo et al. (2021), Bianchi et al. (2021), L'Huillier et al. (2021), Maxted (2022)

# Loan performance recovered quickly after the Great Recession



Source: Senior Loan Officer Opinion Survey (SLOOS) on Bank Lending Practices, Federal Reserve Board

# Expected loan performance took long to recover after the Great Recession



Source: Senior Loan Officer Opinion Survey (SLOOS) on Bank Lending Practices, Federal Reserve Board

## **Bank Expectations:** Senior Loan Officer Opinion Survey of Bank Lending Practices

- Since early 1990s: Inquiring banks about changes in their lending standards & changes in demand for loans ([Bassett et al. \(2014\)](#))
- Since 2004: Inquiring banks' **expectations** on changes in delinquencies & charge-offs in the coming year



## **Bank Expectations:** Senior Loan Officer Opinion Survey of Bank Lending Practices

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- Since 2004: Inquiring banks' **expectations** on changes in delinquencies & charge-offs in the coming year

*Assuming that economic activity progresses in line with consensus forecasts, what is your outlook for delinquencies and charge-offs on your bank's type X loans in the coming year?*

- 1=improve substantially; 2=improve somewhat; 3=remain around current levels; 4=deteriorate somewhat; 5=deteriorate substantially

## Forecast errors:

$$R_{it}^{FE} = E_t[l_{i,t+1}] - l_{i,t+1}$$

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## Bank Expectations: Senior Loan Officer Opinion Survey of Bank Lending Practices

$$E_t[l_{i,t+1}^k] = \begin{cases} 1 & \text{if bank } i \text{ at } t \text{ expects an improvement in type-}k \text{ loan performance in } t+1 \\ 0 & \text{if bank } i \text{ at } t \text{ expects no change in type-}k \text{ loan performance in } t+1 \\ -1 & \text{if bank } i \text{ at } t \text{ expects a worsening in type-}k \text{ loan performance in } t+1 \end{cases}$$

$$E_t[l_{i,t+1}] = \sum_k \omega_{it}^k \times E_t[l_{i,t+1}^k]$$

$\omega_{it}^k$ : fraction of category- $k$  loans outstanding in bank  $i$ 's core loan portfolio.

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## Loan Performance: Call Reports

$$l_{it}^k = \begin{cases} 1 & \text{if bank } i \text{ experiences an improvement in type-}k \text{ loan performance in year } t \\ 0 & \text{if bank } i \text{ experiences no change in type-}k \text{ loan performance in year } t \\ -1 & \text{if bank } i \text{ experiences a worsening in type-}k \text{ loan performance in year } t \end{cases}$$

$$l_{it} = \sum_k \omega_{i,t-1}^k \times l_{it}^k$$

Dynamics of Bank Forecast Errors

$$R_{it}^{FE} = \alpha_i + \sum_{k=1}^K \beta_k R_{it-k}^{FE} + \sum_{k=1}^K g_k X_{it-k} + \tau_t + u_{it}$$

	k=1 year	k=2 year	k=3 year
$\beta_k$	0.233***	0.153***	0.024
[t]	[5.57]	[4.33]	[0.68]
$R^2$		0.59	

- $R_{it}^{FE}$  : forecast errors (< 0: over-pessimistic)
- Sample period: 2010-2020

**Fact 1**: Forecast errors are persistent & positively predictable by lagged forecast errors  
⇒ Pessimism in the past two years breeds pessimism today

► loans

Bank Expectations and Lending Dynamics

$$\Delta Loans_{it} = \alpha_i + \sum_{k=1}^K \beta_k R_{it-k}^{FE} + \sum_{k=1}^K g_k X_{it-k} + \tau_t + u_{it}$$

	k=1 year	k=2 year	k=3 year
$\beta_k$	-0.071	0.239***	0.048
[t]	[-0.52]	[2.96]	[0.55]
$R^2$	0.14		

- $R_{it}^{FE}$ : forecast errors ( $< 0$ : over-pessimistic)
- $\Delta Loans_{it}$ : log change in loans relative to the pre-crisis level
- Sample period: 2010-2020

**Fact 2:** Past forecast errors have significant predictive power for future loan growth, even after controlling for loan demand and tighter regulation

Bank Heterogeneity

$$\Delta Loans_{it} = \alpha_i + \sum_{k=1}^K \beta_k R_{it-k}^{FE} + \sum_{k=1}^K g_k X_{it-k} + \tau_t + u_{it}$$

Small banks (bottom quartile by total loans)			
	k=1 year	k=2 year	k=3 year
$\beta_k$	0.021	0.258*	-0.079
[t]	[0.15]	[1.81]	[-0.86]

Large banks (top quartile by total loans)			
	k=1 year	k=2 year	k=3 year
$\beta_k$	0.246	0.313**	0.121
[t]	[1.46]	[2.36]	[0.82]

Fact 3: The behavioral bias matters more for large banks (and real estate loans)

## Goal

- Quantify the impact of behavioral bias on the slow recovery in lending after 2008



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## Agents

- A continuum of heterogeneous banks
  - Each finances a large number of risky projects (loans)
  - Loan defaults if the collateral value falls below a threshold
- A representative investor owns all banks & prices all loans

## Uncertainty

- $x_{t+1}$ : Bernoulli random variable

$$\text{Prob}(x_{t+1} = 1) = p_t$$

- $p_t$ : aggregate shock  $\Rightarrow$  “disaster risk” (Barro (2006), Gourio (2012, 2013))

$$\log p_{t+1} = (1 - \rho_p) \log \tilde{p} + \rho_p \log p_t + \varepsilon_{p,t+1}$$

- $\omega_{it}$ : bank-specific shock

$$\omega_{i,t+1} = \rho_\omega \omega_{it} + \varepsilon_{\omega i,t+1}$$

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## Expectations

- All agents have full information, but are not fully rational
- Over-extrapolation

$$\text{Prob}^{\mathcal{P}}(x_{t+1} = 1) = p_t^x p_{t-1}^{1-x}$$

$$\log p_{t+1} = (1 - \hat{\rho}_{1p} - \hat{\rho}_{2p}) \log \tilde{p} + \hat{\rho}_{1p} \log p_t + \hat{\rho}_{2p} \log p_{t-1} + \varepsilon_{p,t+1}$$

$$\omega_{i,t+1} = \hat{\rho}_{1\omega} \omega_{it} + \hat{\rho}_{2\omega} \omega_{i,t-1} + \varepsilon_{\omega i,t+1}$$

## Bank's Problem

- Finance loans ( $L$ ) by equity ( $E$ ) and deposits ( $D$ )

$$V^C(L_{i,t-1}, D_{i,t-1}, E_{i,t-1}, \mathbf{s}_{it}) \\ = \max_{Div_{it}, L_{it}} \left\{ Div_{it} + \Lambda(Div_{it}) + E_t^P \left[ M_{t,t+1} \max \left[ V(L_{-it}, D_{it}, E_{it}, \mathbf{s}_{i,t+1}), 0 \right] \middle| \mathbf{s}_{it} \right] \right\}$$

subject to:

$$L_{it} = E_{it} + D_{it}$$

$$E_{it} = E_{it-1} - Div_{it} + r^L(\mathbf{s}_{it}, x_{t+1}, \omega_{i,t+1})L_{it} - r^D D_{it}$$

$$\frac{L_{it}}{E_{it}} \leq \lambda$$

$$\mathbf{s}_{it} = \{p_t, \omega_{it}, p_{t-1}, \omega_{i,t-1}\}$$

► payoff

► SDF

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- Finance loans ( $L$ ) by equity ( $E$ ) and deposits ( $D$ )
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- Finance loans ( $L$ ) by equity ( $E$ ) and deposits ( $D$ )
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$$V^C(L_{i,t-1}, D_{i,t-1}, E_{i,t-1}, \mathbf{s}_{it}) = \max_{Div_{it}, L_{it}} \left\{ Div_{it} + \Lambda(Div_{it}) + E_t^P \left[ M_{t,t+1} \max \left[ V(L_{it}, D_{it}, E_{it}, \mathbf{s}_{i,t+1}), 0 \right] \middle| \mathbf{s}_{it} \right] \right\}$$

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- Finance loans ( $L$ ) by equity ( $E$ ) and deposits ( $D$ )
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- Default if the continuation value becomes too low

$$V^C(L_{i,t-1}, D_{i,t-1}, E_{i,t-1}, \mathbf{s}_{it}) = \max_{Div_{it}, L_{it}} \left\{ Div_{it} + \Lambda(Div_{it}) + E_t^P \left[ M_{t,t+1} \max \left[ V(L_{it}, D_{it}, E_{it}, \mathbf{s}_{i,t+1}), 0 \right] \mid \mathbf{s}_{it} \right] \right\}$$

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## Bank's Problem

- Finance loans ( $L$ ) by equity ( $E$ ) and deposits ( $D$ )
- Accumulate equity through retained earnings
- Face a capital requirement constraint
- Default if the continuation value becomes too low
- **Biased beliefs affect the return on loans and expected continuation value**

$$V^C(L_{i,t-1}, D_{i,t-1}, E_{i,t-1}, \mathbf{s}_{it}) = \max_{D_{it}, L_{it}} \left\{ Div_{it} + \Lambda(Div_{it}) + \mathbf{E}_t^P \left[ M_{t,t+1} \max \left[ V(L_{it}, D_{it}, E_{it}, \mathbf{s}_{i,t+1}), 0 \right] \middle| \mathbf{s}_{it} \right] \right\}$$

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$$\mathbf{s}_{it} = \{\mathbf{p}_t, \omega_{it}, \mathbf{p}_{t-1}, \omega_{i,t-1}\}$$

► payoff

► SDF



## Bringing Model to Data

- Calibrate two variants of the model at an annual frequency: OE and RE
- All shocks are determined according to their true processes
- Targeted moments: leverage, profit-to-equity, bank default rate, **dynamics of bank forecast errors**  $\Rightarrow$  **AR(2)** 

## Bringing Model to Data

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- All shocks are determined according to their true processes
- Targeted moments: leverage, profit-to-equity, bank default rate, dynamics of bank forecast errors  $\Rightarrow$  AR(2) [▶ target](#)
- Untargeted moments: business cycle correlations + autocorrelations of
  - Loan growth
  - Change in expected loan performance
  - Loan rate growth

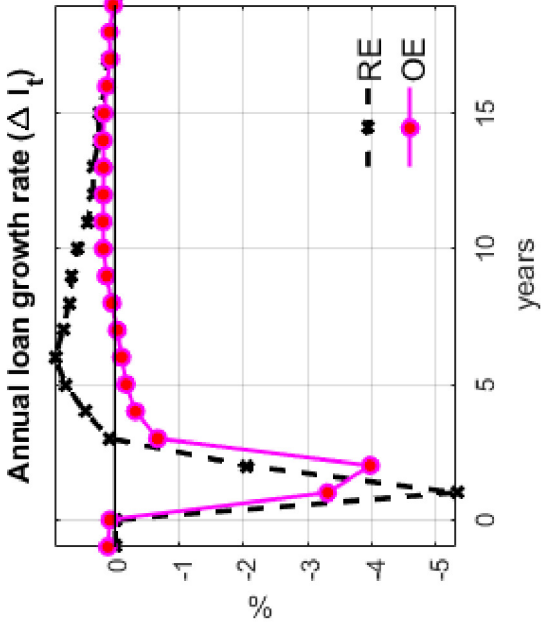
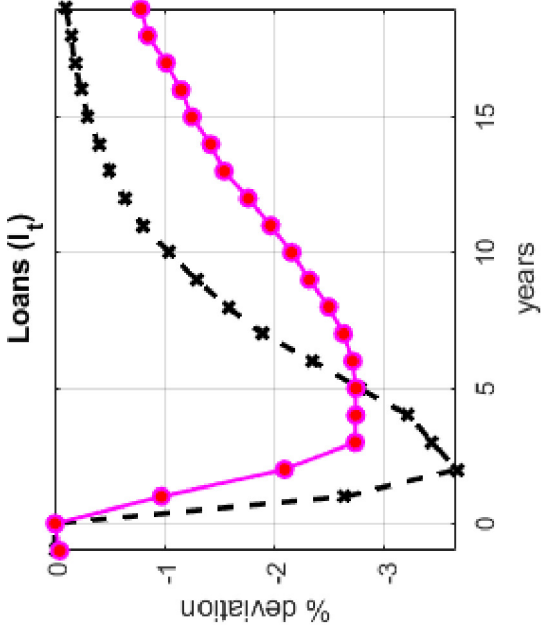
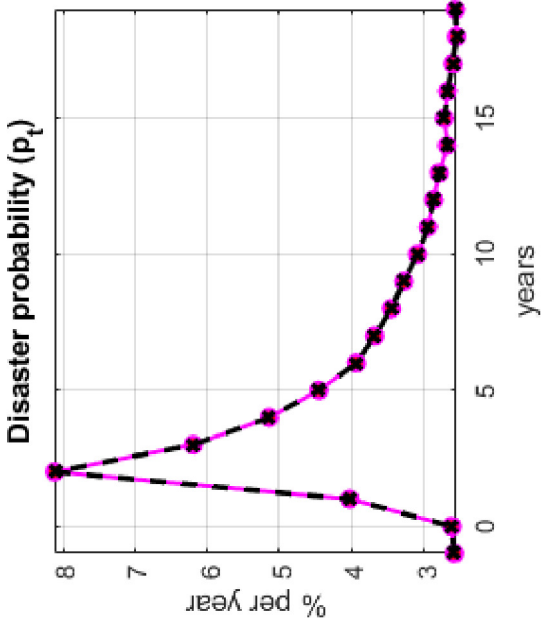
**Goal:** Test the business cycle properties of bank behavior

[▶ moments](#)

## Main Exercise

- We model the 2008-09 financial crisis as two consecutive positive shocks to the disaster probability
- Look at the responses of aggregate loan growth, bank value, expectations
- Look at the counterfactual exercise (under rational expectations) to understand the impact of overextrapolation
- Look at the responses of large vs. small banks (defined by size of loan portfolio)

IRF to a Temporary Increase in Disaster Probability



	Data	OE	RE
Years taken for the recovery of loan growth	7	7	3
Net fraction of banks expect worsening	8	8	5

► IRF

► disaster

## Mechanism

$$L(L_{i,t-1}, E_{i,t-1}, p_t, \omega_{it}, p_{t-1}, \omega_{i,t-1})$$

- **Bias:** Lending is decreasing in  $p_t$  as well as  $p_{t-1}$ 
  - Even when the disaster probability starts to decrease, bank lending continues to decline

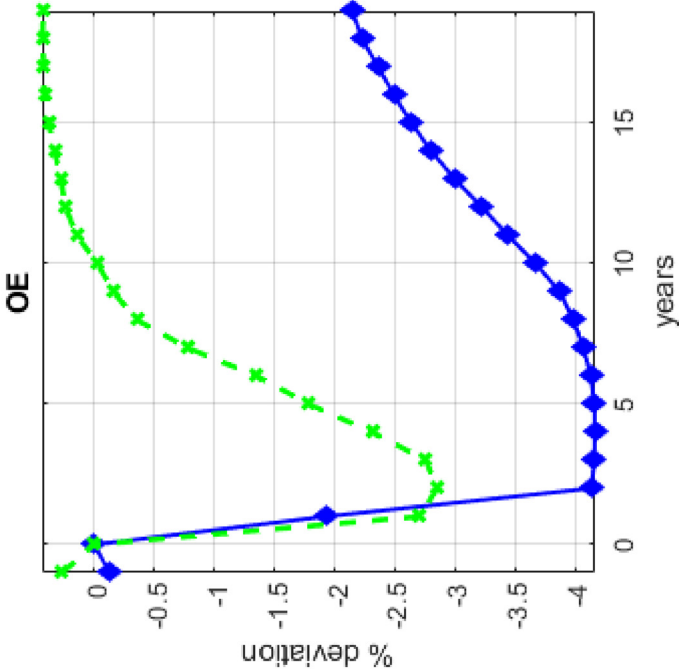
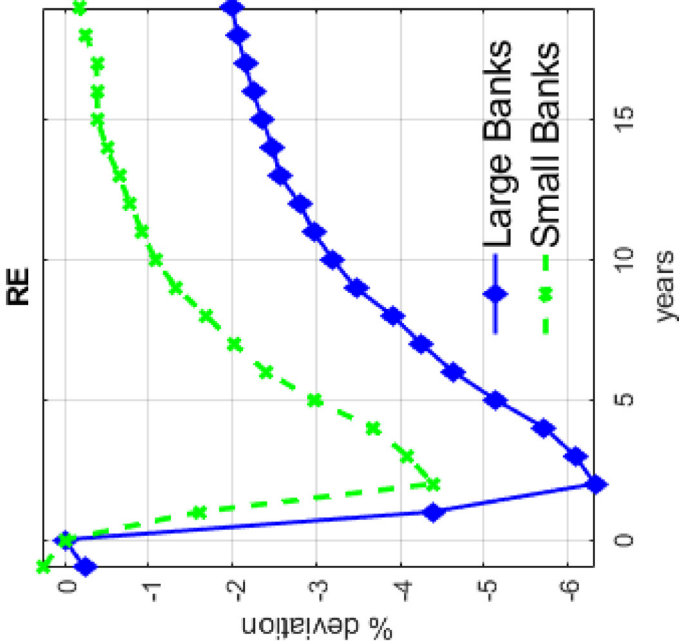
## Mechanism

$$L\left(L_{i,t-1}, E_{i,t-1}, p_t, \omega_{it}, p_{t-1}, \omega_{i,t-1}\right)$$

- Bias: Lending is decreasing in  $p_t$  as well as  $p_{t-1}$ 
  - Even when the disaster probability starts to decrease, bank lending continues to decline
- **Bias + balance sheet constraint:** Realized loan return ( $r_{it}$ ) increases more slowly as disaster probability decreases
  - Profit & equity ( $E_{it}$ ) recover more slowly
  - Lending increases more slowly

► AR(2) intuition

**IRF of Lending to a Temporary Increase in Disaster Probability**  
**(Large vs. Small Banks)**



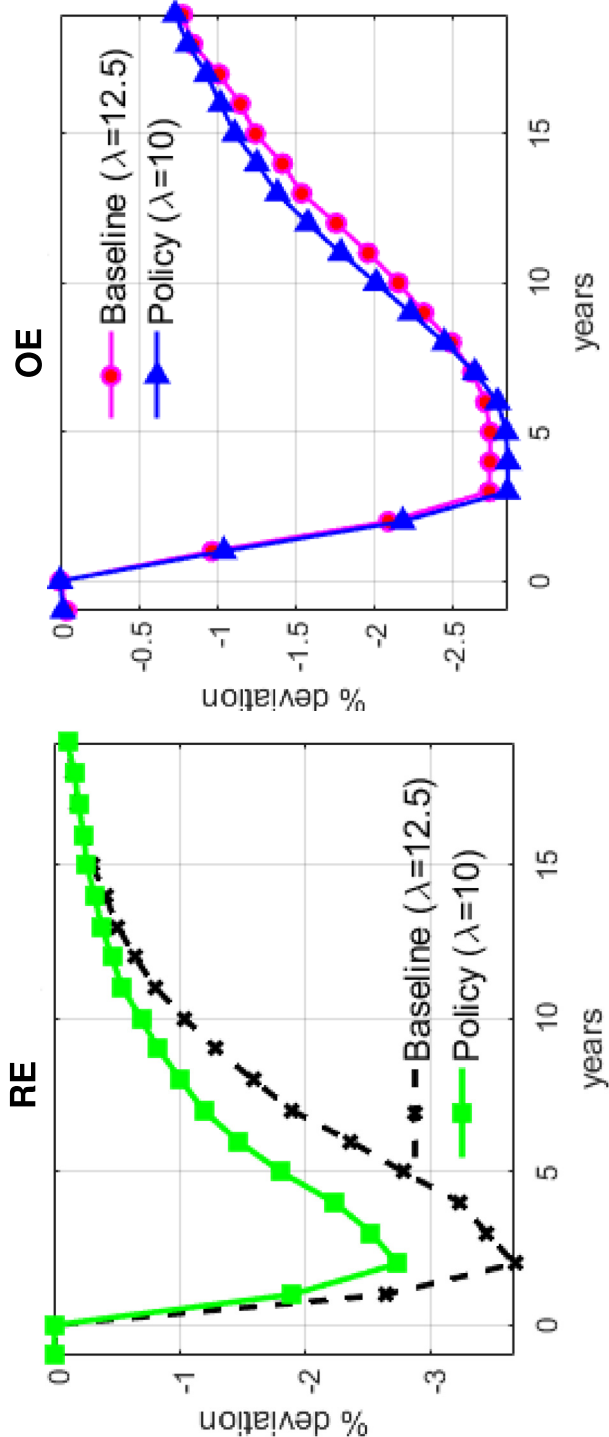
### Additional Exercises: Policy Impact

- Capital requirement: increase the minimum equity-to-asset ratio from 8% to 10%
- Monetary policy: lower  $r^D$  by 10 basis points



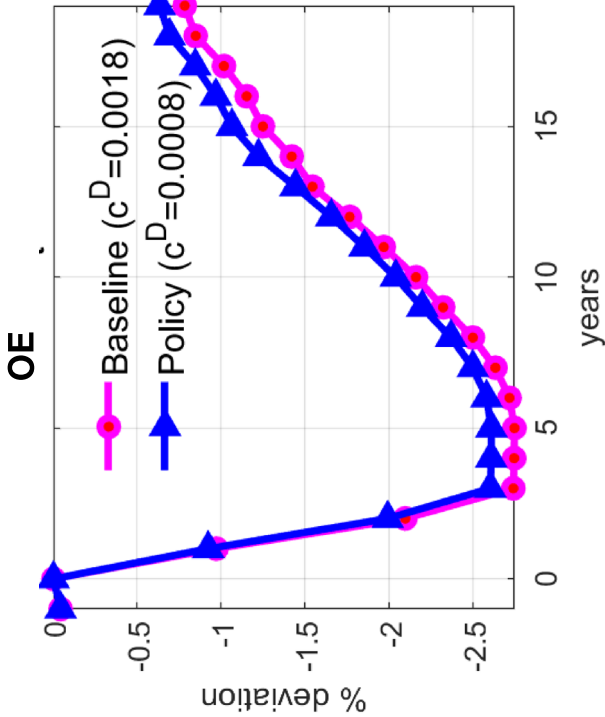
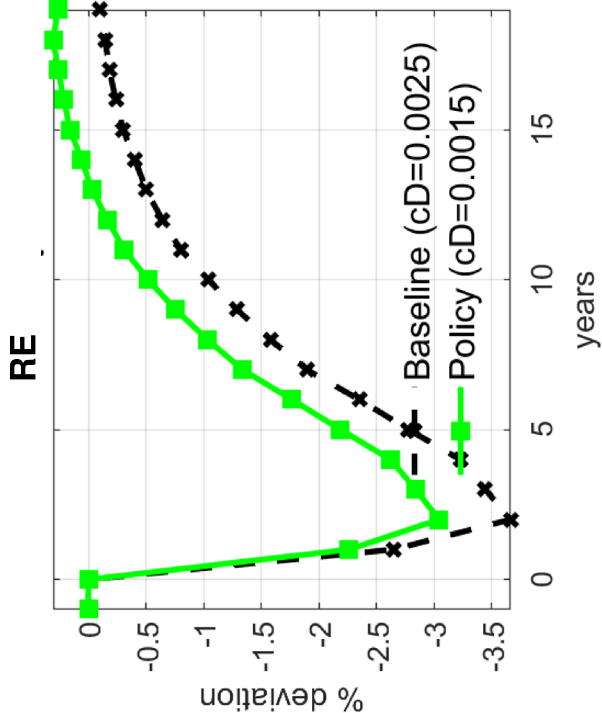
# IRF of Lending to a Temporary Increase in Disaster Probability

## Higher Capital Requirement



# IRF of Lending to a Temporary Increase in Disaster Probability

## Lower Bank Funding Cost



# To Conclude

- Bank expectations are distorted – lasting pessimism
- And they matter for lending decisions – contribute to lending slumps
- Lasting bank pessimism also hampers the effectiveness of financial policies (QE, etc)

**Table:** Dynamics of Bank Forecast Errors and Loan Performance

$$R_{it}^{FE} = \alpha_i + \sum_{k=1}^K \beta_k R_{it-k}^{FE} + \sum_{k=1}^K g_k X_{it-k} + \tau_t + u_{it}$$

	Forecast Errors			Loan Performance		
	k=1 year	k=2 year	k=3 year	k=1 year	k=2 year	k=3 year
$\beta_k$	0.233***	0.153***	0.024	0.064	-0.070**	-0.086***
[t]	[5.57]	[4.33]	[0.68]	[0.70]	[-2.16]	[-3.36]
$R^2$	0.59			0.42		

► Back

**Table:** Bank Expectations and Lending Dynamics, Controlling for Alternatives

$$\Delta Loans_{it} = \alpha_j + \sum_{k=1}^K \beta_k R_{it-k}^{FE} + \sum_{k=1}^K g_k X_{it-k} + \tau_t + u_{it}$$

	Loan Demand			Crisis Loan Performance		
	k=1 year (1)	k=2 year (2)	k=3 year (3)	k=1 year (4)	k=2 year (5)	k=3 year (6)
$\beta_k$ [t]	-0.141 [-0.97]	0.220*** [2.64]	0.053 [0.58]	-0.169 [-0.95]	0.236** [2.36]	0.039 [0.45]
$Control_k$ [t]	0.053 [0.60]	0.092 [1.39]	0.120** [2.42]	-0.200 [-0.95]	0.465* [1.93]	-0.187 [-0.62]
	Bank Capital			Bank Liquidity		
	k=1 year (1)	k=2 year (2)	k=3 year (3)	k=1 year (4)	k=2 year (5)	k=3 year (6)
$\beta_k$ [t]	-0.067 [-0.48]	0.239*** [2.96]	0.048 [0.55]	-0.075 [-0.52]	0.245*** [2.87]	0.043 [0.46]
$Control_k$ [t]	0.114 [0.77]	-0.182 [-1.48]	-0.053 [-0.49]	0.116** [2.07]	-0.085** [-2.09]	-0.041 [-0.57]

[► Back](#)

**Table:** Bank Expectations and Lending Dynamics

$$\Delta Loans_{it} = \alpha_i + \sum_{k=1}^K \beta_k R_{it-k}^{FE} + \sum_{k=1}^K g_k X_{it-k} + \tau_t + u_{it}$$

	Forecast Errors			Loan Performance		
	k=1 year (1)	k=2 year (2)	k=3 year (3)	k=1 year (4)	k=2 year (5)	k=3 year (6)
$\beta_k$						
	-0.071	0.239***	0.048			
[t]	[-0.52]	[2.96]	[0.55]			
$g_k$						
				-0.161	-0.199***	-0.170**
[t]				[-0.89]	[-2.49]	[-3.03]
$R^2$	0.14					

► Back

**Table:** Loan Heterogeneity

C&I Loans				RRE Loans		
	k=1 year	k=2 year	k=3 year	k=1 year	k=2 year	k=3 year
$\beta_k^{\text{own}}$	0.023	0.025*	0.032	-0.021	0.092**	-0.045
[t]	[1.48]	[1.88]	[1.52]	[-0.30]	[2.37]	[-0.39]
$\beta_k^{\text{other}}$	0.021	0.015	0.021	0.050	0.036	0.037
[t]	[0.89]	[0.64]	[1.17]	[0.35]	[0.50]	[0.39]
Consumer Loans						
	k=1 year	k=2 year	k=3 year	k=1 year	k=2 year	k=3 year
$\beta_k^{\text{own}}$	0.091	0.111*	0.121	-0.212	0.005	0.125
[t]	[1.47]	[2.59]	[1.40]	[-1.25]	[0.03]	[-0.65]
$\beta_k^{\text{other}}$	-0.121	0.065	-0.010	0.042	0.215	0.142
[t]	[1.27]	[0.83]	[-0.14]	[0.29]	[1.40]	[1.15]

► Back

Table: Additional Heterogeneity

$$R_{it}^{FE} = \alpha_i + \sum_{k=1}^K \beta_k R_{it-k}^{FE} + \sum_{k=1}^K g_k X_{it-k} + \tau_t + u_{it}$$

	Small Banks			Large Banks		
	k=1 year (1)	k=2 year (2)	k=3 year (3)	k=1 year (4)	k=2 year (5)	k=3 year (6)
$\beta_k$ [t]	0.254** [2.15]	0.121* [1.73]	0.107 [1.28]	0.308** [4.64]	0.138** [2.14]	-0.046 [-0.70]

► Back



## Loan Portfolio

- Each bank holds an equal-weighted portfolio of a large number of loans
- Borrower  $j$  defaults on bank  $i$  at time  $t$  if  $W_{ijt} < \kappa$ . The bank can recover a fraction  $1 - \mathcal{L}$  of the collateral value

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- Borrower  $j$  defaults on bank  $i$  at time  $t$  if  $W_{ijt} < \kappa$ . The bank can recover a fraction  $1 - \mathcal{L}$  of the collateral value
- Payoff, price and return of loan portfolio:

$$\pi_{i,t+1}^L(\varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1}) = \underbrace{\kappa \text{Prob}\left(W_{ij,t+1} \geq \kappa \mid \varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1}\right)}_{\text{Repay}} + \underbrace{(1 - \mathcal{L})\text{E}\left[W_{ij,t+1} \mathbb{1}_{W_{ij,t+1} < \kappa} \mid \varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1}\right]}_{\text{Default}}$$

## Loan Portfolio

- Each bank holds an equal-weighted portfolio of a large number of loans
- Borrower  $j$  defaults on bank  $i$  at time  $t$  if  $W_{ijt} < \kappa$ . The bank can recover a fraction  $1 - \mathcal{L}$  of the collateral value
- Payoff, price and return of loan portfolio:

$$\pi_{i,t+1}^L(\varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1}) = \underbrace{\kappa \text{Prob}\left(W_{ij,t+1} \geq \kappa \mid \varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1}\right)}_{\text{Repay}} + \underbrace{(1 - \mathcal{L})\text{E}\left[W_{ij,t+1} \mathbb{1}_{W_{ij,t+1} < \kappa} \mid \varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1}\right]}_{\text{Default}}$$

$$P_{it}^L(\mathbf{s}_{it}) = \text{E}_t^{\mathcal{P}} \left[ M_{t,t+1} \pi_{i,t+1}^L(\varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1}) \right].$$

$$r_{i,t+1}^L(\mathbf{s}_{it}, \varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1}) = \frac{\pi_{i,t+1}^L(\varepsilon_{c,t+1}, X_{t+1}, \omega_{i,t+1})}{P_{it}^L(\mathbf{s}_{it})} - 1$$

$\mathbf{s}_{it}$ : exogenous states (depend on belief process)

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## Endowment & Preferences

- Baseline model: exogenous process for consumption

$$C_{t+1} = C_t e^{\mu_c + \sigma_c \varepsilon_{c,t+1} + \xi X_{t+1}}$$

- Stochastic discount factor (Epstein-Zin preferences)

$$M_{t,t+1} = \beta^\theta \left( \frac{C_{t+1}}{C_t} \right)^{-\gamma} \left( \frac{S_{t+1} + 1}{S_t} \right)^{-1+\theta}, \quad \theta = \frac{1-\gamma}{1-\gamma/\psi}$$

- Consumption-wealth ratio  $S_t$

$$\mathbb{E}_t^{\mathcal{P}} \left[ \beta^\theta \left( \frac{C_{t+1}}{C_t} \right)^{1-\gamma} (S_{t+1} + 1)^\theta \right] = S_t^\theta$$

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**Table:** Targeted Moments

Description	Data	OE	RE
Leverage (mean)	8.50	8.72	8.69
Leverage (std)	2.95	3.10	2.50
Profit-to-equity (mean)	0.169	0.137	0.149
Bank default rate (mean)	0.041	0.062	0.053
Dynamics of bank forecast errors			
1-year	0.233	0.243	—
2-year	0.153	0.169	—

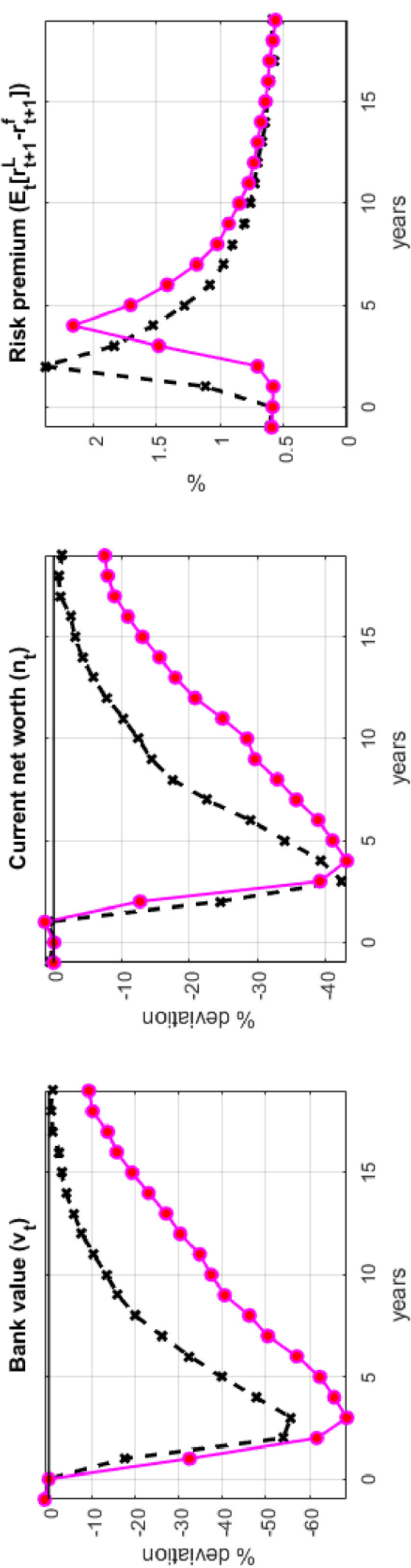
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## Untargeted Moments

	Data	OE	RE
<b>Annual loan growth</b>			
$\text{Corr}(\Delta L_t, \Delta \text{GDP}_{t-1})$	0.239	0.135	-0.015
$\text{Corr}(\Delta L_t, \Delta \text{GDP}_{t-2})$	0.218	0.056	-0.136
$\text{Corr}(\Delta L_t, \Delta l_{t-1})$	0.207	0.597	0.123
$\text{Corr}(\Delta L_t, \Delta l_{t-2})$	0.118	0.160	-0.036
<b>Annual change in expected loan performance</b>			
$\text{Corr}(\Delta E_t[\text{LoanDefault}_{t+1}], \Delta \text{GDP}_{t-1})$	-0.023	-0.077	0.192
$\text{Corr}(\Delta E_t[\text{LoanDefault}_{t+1}], \Delta \text{GDP}_{t-2})$	0.295	0.230	0.134
$\text{Corr}(\Delta E_t[\text{LoanDefault}_{t+1}], \Delta E_{t-1}[\text{LoanDefault}_t])$	0.465	0.197	-0.152
$\text{Corr}(\Delta E_t[\text{LoanDefault}_{t+1}], \Delta E_{t-2}[\text{LoanDefault}_{t-1}])$	0.153	0.082	-0.094
<b>Annual loan rate growth</b>			
$\text{Corr}(\Delta E_t[r_{t+1}^L], \Delta \text{GDP}_{t-1})$	0.071	0.110	-0.301
$\text{Corr}(\Delta E_t[r_{t+1}^L], \Delta \text{GDP}_{t-2})$	0.022	0.009	-0.270
$\text{Corr}(\Delta E_t[r_{t+1}^L], \Delta E_{t-1}[r_t^L])$	0.017	0.177	-0.141
$\text{Corr}(\Delta E_t[r_{t+1}^L], \Delta E_{t-2}[r_{t-1}^L])$	-0.013	-0.072	-0.109

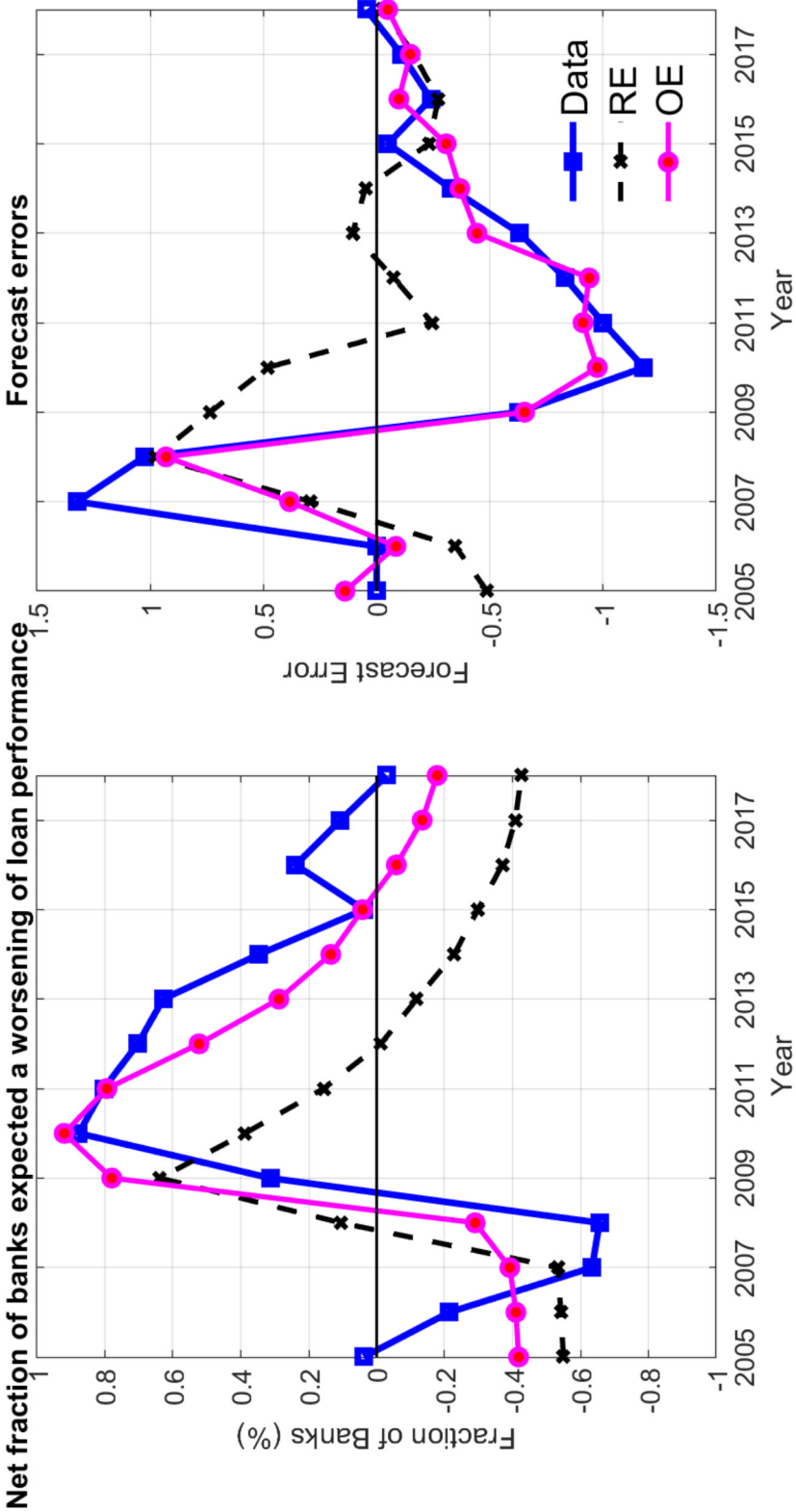
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**Figure:** IRF to a Temporary Increase in Disaster Probability



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**Figure:** IRF to a Temporary Increase in Disaster Probability

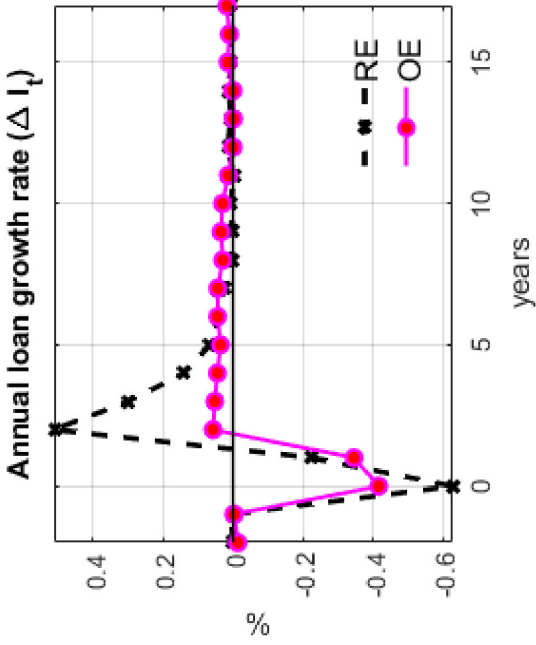
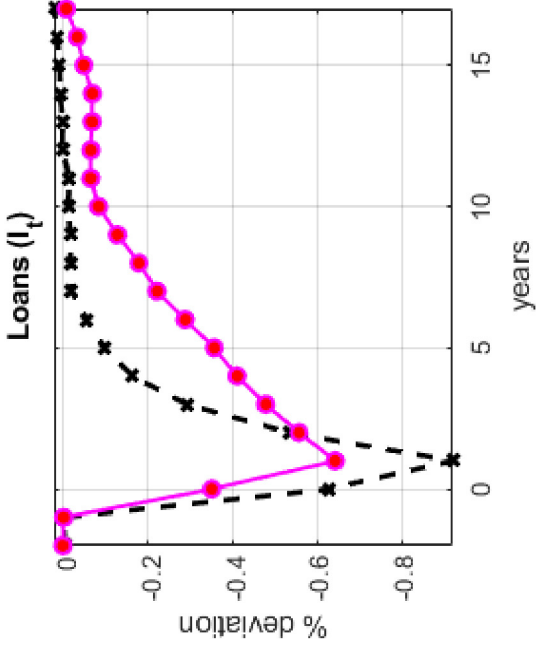
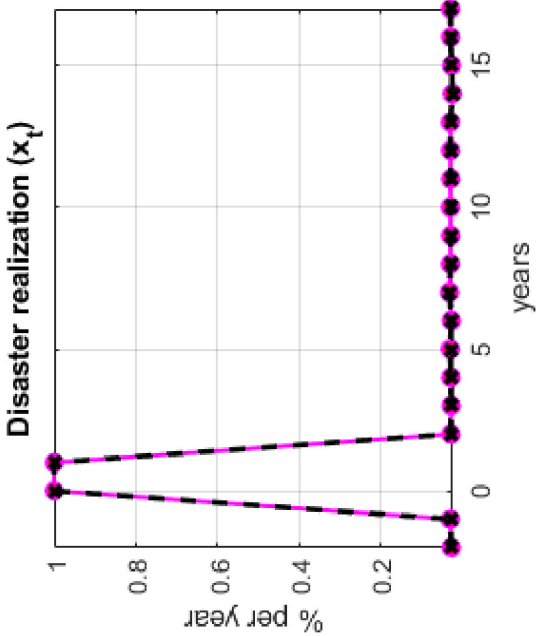


Number of years taken for the recovery of:	Data	OE	RE
Net fraction of banks experience worsening	3	5	5
Net fraction of banks expect worsening	8	8	5

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Figure: Disaster in the Model



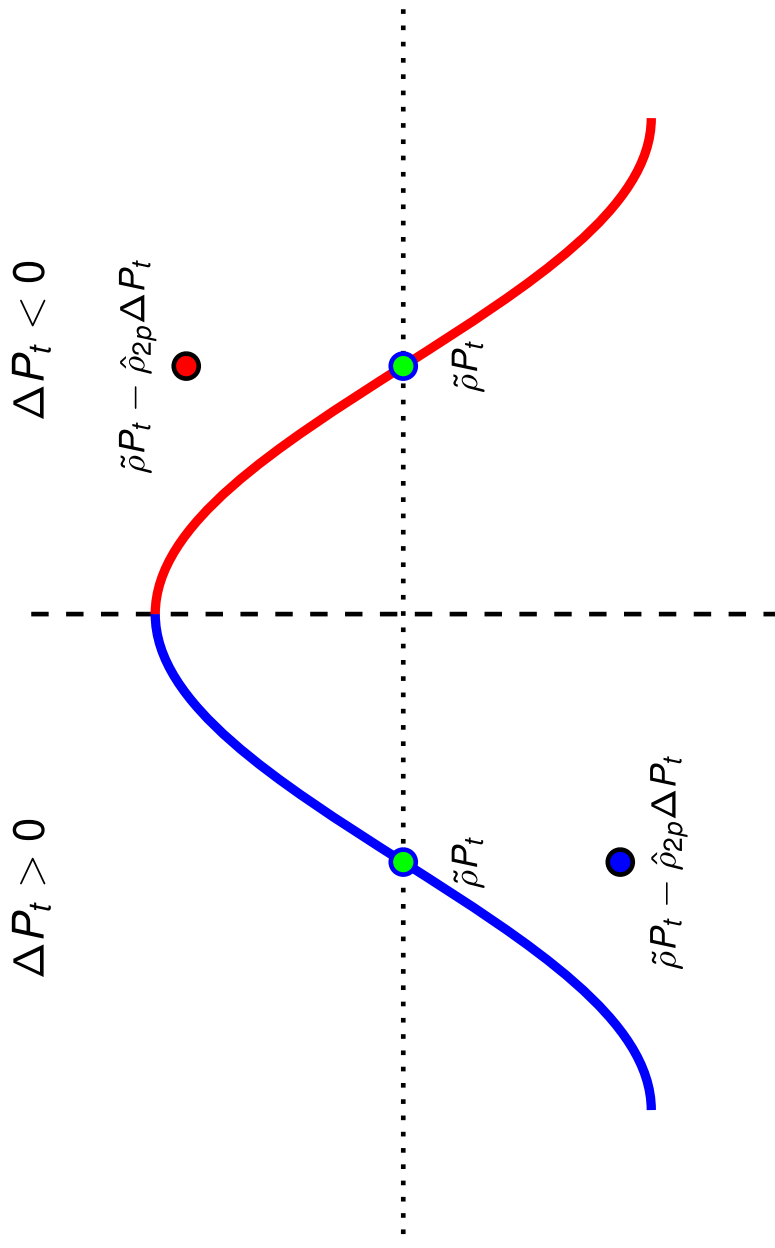
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## OE: AR(2) or AR(1) with higher persistence?

Let  $P_t \equiv \log p_t$ :

$$\begin{aligned} P_{t+1} &= (1 - \hat{\rho}_{1p} - \hat{\rho}_{2p})\tilde{P} + \hat{\rho}_{1p}P_t + \hat{\rho}_{2p}P_{t-1} + \varepsilon_{p,t+1} \\ &= (1 - \hat{\rho}_{1p} - \hat{\rho}_{2p})\tilde{P} + (\hat{\rho}_{1p} + \hat{\rho}_{2p})P_t - \hat{\rho}_{2p}\Delta P_t + \varepsilon_{p,t+1} \\ &= (1 - \tilde{\rho}_p)\tilde{P} + \underbrace{\tilde{\rho}_p P_t - \hat{\rho}_{2p}\Delta P_t}_{\text{momentum}} + \varepsilon_{p,t+1} \end{aligned}$$

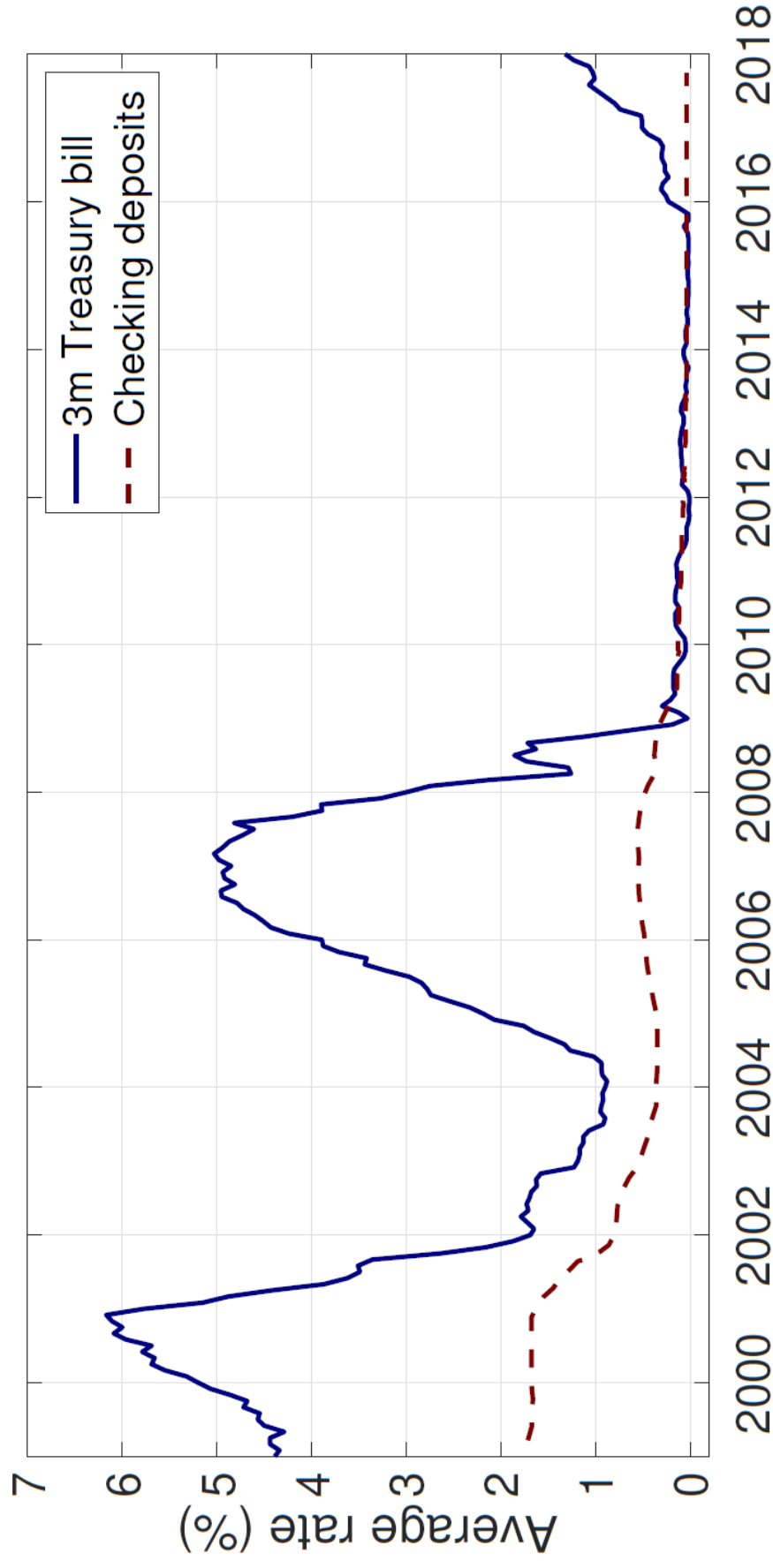
- AR(1): only current state of the economy ( $P_t$ ) matters for expectation formation, regardless of whether  $\tilde{\rho}_p$  is the true coefficient
- AR(2): captures an asymmetry, depending on where the economy has been



- Over-extrapolation under AR(1)
- Over-extrapolation under AR(2), with  $\Delta P_t > 0$  and  $\hat{\rho}_{2p} > 0 \implies$  at the end of a boom
- Over-extrapolation under AR(2), with  $\Delta P_t < 0$  and  $\hat{\rho}_{2p} > 0 \implies$  at the end of a crisis

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**Figure: Rates on Deposits**



Sources: Gomes, Grotteria and Wachter (2020)